

# Uncovering the mechanism of chiral three-nucleon force in driving spin-orbit splitting<sup>†</sup>

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Three-nucleon forces (3NFs) play a crucial role in describing various phenomena of nuclei. For example, the 3NF enhances the spin-orbit (SO) splitting, as indicated in the literature.<sup>1–8)</sup> However, the detailed mechanism by which the 3NF contributes to SO splitting has not been fully clarified.

To uncover the aforementioned mechanism, we employed the state-of-the-art 3NFs derived from chiral effective field theory at next-to-next-to-leading order (N<sup>2</sup>LO) and decomposed them in terms of the rank of the irreducible tensors forming the three-nucleon potentials. The tensorial structure of the chiral-N<sup>2</sup>LO 3NF is summarized in Fig. 1. The decomposed 3NFs were then implemented in the shell-model calculations.<sup>9)</sup>

We clarified that the rank-1 component of the 3NF contributes dominantly to the SO splitting of *p*-shell nuclei. This is because the rank-1 3NF generates a one-body SO potential, the density dependence of which differs from that originating from the two-nucleon SO force.<sup>2)</sup> As shown in Fig. 1, the rank-1 3NF arises solely from the two-pion ( $2\pi$ )-exchange process. The low-energy constants (LECs) of the  $2\pi$ -exchange potentials are relatively well constrained from pion-nucleon scattering compared to those of one-pion ( $1\pi$ )-exchange and contact (ct) terms. Therefore, our conclusion is expected to be robust against the uncertainty of the short-range LECs.

We also revealed an important property of the rank-1 3NF, *i.e.*, an antisymmetric SO (ASO) interaction. The ASO 3NF affects the two-nucleon spin states, which are associated with the subsystem of three-nucleon systems. In particular, the ASO 3NF mixes the singlet and triplet states of two-nucleon spin states, and thus, it can change the quantum entanglement of spin states. Furthermore, the ASO 3NF induces two-nucleon spin canting, similar to the spin canting of magnetic ions driven by the Dzyaloshinsky-Moriya interaction.<sup>10–12)</sup>

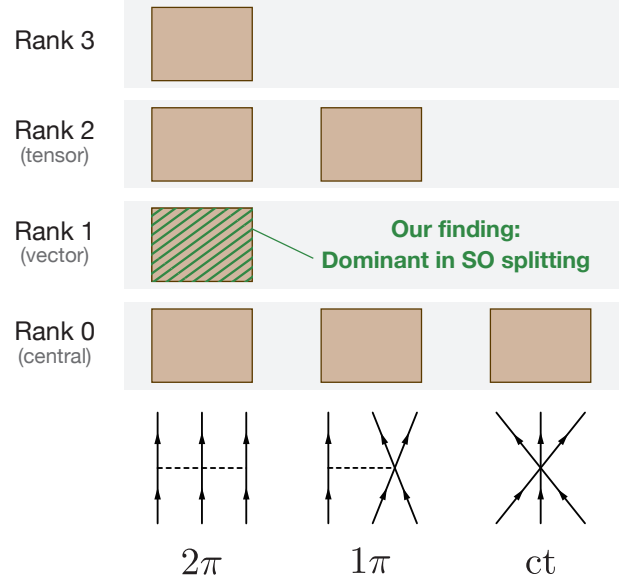


Fig. 1. Classification of chiral 3NF at N<sup>2</sup>LO in terms of the rank of tensors forming the potential. We found that the rank-1 component originating from the  $2\pi$ -exchange process essentially contributes to the SO splitting of light nuclei, whereas  $1\pi$ -exchange and contact terms were found to have a marginal effect.

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